

# Spectral Delay Filters\*

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This paper discusses the implementation of spectral delay using filters comprising a cascade of many low-order allpass filters and an equalizing filter. The spectral delay filters have chirp-like impulse responses causing a large, frequency-dependent delay that is useful in audio effects processing. An equalizing filter design and a multirate technique, which stretches the allpass filters, impulse response, are introduced.

## 0 INTRODUCTION

Filtering an audio signal with an allpass filter does not usually have a major effect on the signal's timbre. The allpass filter does not change the frequency content of the signal, but only introduces a phase shift or delay. Audibility of the phase distortion caused by an allpass filter in a sound reproduction system has been a topic of many studies, see, e.g., [1], [2]. In this paper, we investigate audio effects processing using high-order allpass filters that consist of many cascaded low-order allpass filters. These filters have long chirp-like impulse responses. When audio and music signals are processed with such a filter, remarkable changes are obtained that are similar to the spectral delay effect [3], [4].

## 1 CHIRP-LIKE IMPULSE RESPONSES AND GROUP DELAY

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$$A(z) = \frac{a_1 + z^{-1}}{1 + a_1 z^{-1}}, \quad (1)$$

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$$\tau_{g,\max} = \begin{cases} \tau_g(0) = \frac{1-a_1}{1+a_1}, & \text{when } a_1 \leq 0 \\ \tau_g(\pi) = \frac{1+a_1}{1-a_1}, & \text{when } a_1 > 0. \end{cases} \quad (2)$$

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- 1) Green-function determined experimentally and published.
- 2) Black-function determined using similarity searches and published.
- 3) Red-function determined using similarity searches and determined in this study.
- 4) Blue-O-antigen structure unknown. Function determined using similarity searches and proposed in this study.

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Table 1. Active sites and allosteric sites of the GNE MNK enzyme

Excerpt No.	Genre	Spatial Mode	Correlation
1	Pop	FB	94%
2	Classical	FB	33%
3	Jazz	FF	76%
4	Arabian	FF	41%
5	GNE	H220	45%
6	GNE	H45	93%
7	MNK	G416	74%
8	MNK	D413	72%
9	MNK	R420	94%
10	MNK	N516	91%

Note. This table does not include sentence enhancement statutes. This table does not include sentence enhancement statutes.

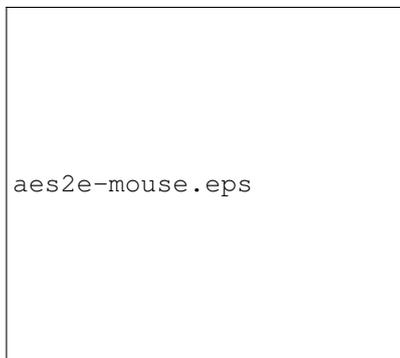


Fig. 1. The spectral delay filter consists of  $M$  allpass filters and an equalization filter.

<sup>1</sup>This point is emphasized by Loewer, see esp. p. (610).

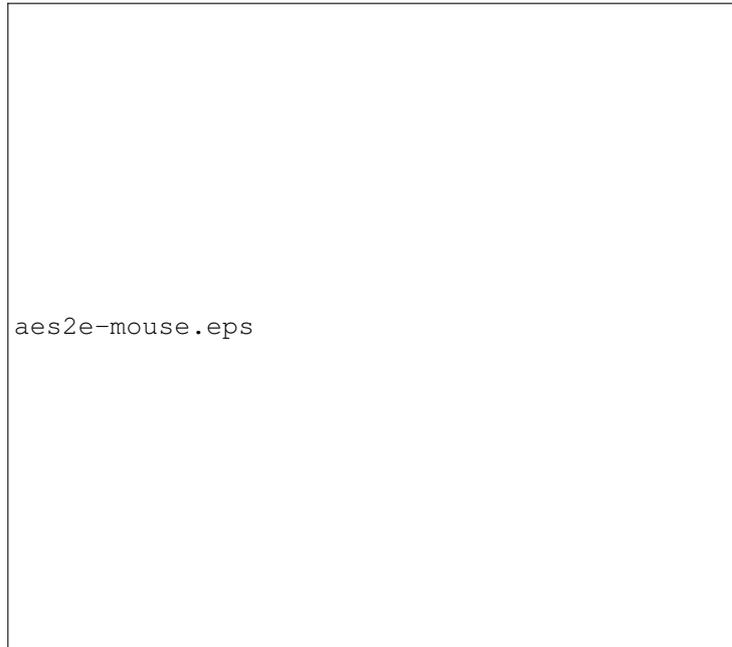


Fig. 2. This paper is organized as follows. In Section 1, we discuss the group delay of a cascade of first-order allpass filters and its relation to the chirp-like impulse response of the spectral delay filter. Furthermore, a multirate method to stretch the impulse response of the spectral delay filter is proposed. Section 2 discusses the amplitude envelope of the impulse response and suggests a design method for the equalizing filter. Section 3 presents application examples using the spectral delay filter. Section 4 concludes this paper.

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$$\tau_g(\omega) = -\frac{d\phi(\omega)}{d\omega}.$$

Audibility of the phase distortion caused by an allpass filter in a sound reproduction system has been a topic of many studies, see, e.g., [1], [2]. In this paper, we investigate audio effects processing using high-order allpass filters that consist of many cascaded low-order allpass filters. These filters have long chirp-like impulse responses. When audio and music signals are processed with such a filter, remarkable changes are obtained that are similar to the spectral delay effect.

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## 2 SUMMARY

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## 3 CONCLUSION

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## 4 ACKNOWLEDGMENT

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## 5 REFERENCES

- [1] D. Preis, "Phase Distortion and Phase Equalization in Audio Signal Processing—A Tutorial Review," *J. Audio Eng. Soc.*, vol. 30, no. 11, pp. 774–779 (1982 Nov.).
- [2] J. S. Abel, D. P. Berners, "MUS424/EE367D: Signal Processing Techniques for Digital Audio Effects," (2005), unpublished Course Notes, CCRMA, Stanford University, Stanford, CA.
- [3] C. Roads, "Musical Sound Transformation by Convolution," presented at the *Int. Computer Music Conf.*, pp. 102–109 (1993).
- [4] C. Roads, *The Computer Music Tutorial* (MIT Press, Cambridge, MA), 1st ed. (1996).
- [5] H. Morgenstern, B. Rafaely, "Spatial Reverberation and Dereverberation Using an Acoustic Multiple-Input Multiple-Output System," *J. Audio Eng. Soc.*, vol. 65, no. 1/2, pp. 42–55 (2017 Jan.Feb.), [Online]. Available: <https://doi.org/10.17743/jaes.2016.0063>.

## APPENDIX

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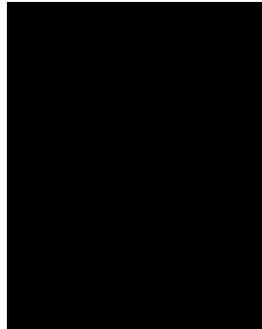
$$\phi(\omega) = -\omega + 2 \arctan \left( \frac{a_1 \sin \omega}{1 + a_1 \cos \omega} \right) \quad (1)$$

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**NOMENCLATURE**

$a_c$  = condensation coefficient  
condensation coefficient

TLR = Toll-like receptor  
PAMPs = pathogen-associated molecular patterns  
condensation coefficient

**THE AUTHORS**

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A1firstname A1lastname is professor of audio signal processing at Helsinki University of Technology (TKK), Espoo, Finland. He received his Master of Science in Technology, Licentiate of Science in Technology, and Doctor of Science in Technology degrees in electrical engineering from TKK in 1992, 1994, and 1995, respectively. His doctoral dissertation dealt with fractional delay filters and physical modeling of musical wind instruments. Since 1990, he has worked mostly at TKK with the exception of a few periods. In 1996 he spent six months as a postdoctoral research fellow at the University of Westminster, London, UK. In 2001-2002 he was professor of signal processing at the Pori School of Technology and Economics, Tampere University of Technology, Pori, Finland. During the academic year 2008-2009 he has been on sabbatical and has spent several months as a visiting scholar at the Center for Computer Research in Music and Acoustics (CCRMA), Stanford University, Stanford, CA. His research interests include musical signal processing, digital filter design, and acoustics of musical instruments. Prof. Välimäki is a senior member of the IEEE Signal Processing Society and is a member of the AES, the Acoustical Society of Finland, and the Finnish Musicological Society. He was the chairman of the 11th International Conference on Digital Audio Effects (DAFx-08), which was held in Espoo, Finland, in 2008.



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